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**TITLE:** MIXING RULES FOR AND EFFECTS OF OTHER HYDROGEN ISOTOPES AND OF ISOTOPIC SWAMPING ON TRITIUM RECOVERY AND LOSS TO BIOSPHERE FROM FUSION REACTORS

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Efficient recovery of bred and unburnt tritium is essential for maintaining low tritium inventories. Escape of tritium to the biosphere can be minimized by maintaining low tritium inventories and by providing engineering barriers to tritium escape. Under emergency conditions, the breeding blanket and the main coolant loops are usually considered to represent the greatest hazard. Whereas during normal operations, thin, hot reactor components lying under direct paths to the biosphere are critical to tritium escape, tritium escape into steam cycle loops, and thence into the biosphere, is generally regarded to be the most important pathway to be dealt with. Normal fuel cycle operations in power plants require a high degree of tritium recovery and escape-prevention barriers.

Protium will be generated by fission reactions of  $^{235}\text{U}$  and  $^{239}\text{Pu}$  in the reactor core. The amount of protium generated is proportional to the amount of fuel burned. Protium is a gas at normal temperatures and pressures and is highly mobile. It is a strong reducing agent and is highly reactive with many materials. It is a strong neutron absorber and is a strong poison. It is a strong oxidizing agent and is a strong poison. It is a strong neutron absorber and is a strong poison. It is a strong oxidizing agent and is a strong poison.

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and deuterium. Thus, unburnt tritium and deuterium, which constitute the majority of fuel fed to fusion reactors, may not represent the majority of hydrogen isotopes recovered.

Recovery of deuterium, which is relatively abundant in nature and can be obtained at modest cost, is not necessary for economic generation of fusion energy. However, buildup of protium and deuterium within reactor subsystems to excessive levels cannot be tolerated, because of potential deleterious effects on reactor materials of construction. Tritium recovery systems will simultaneously remove protium and deuterium because of their similar physicochemical characteristics, but at a penalty of increased tritium recovery system capacity.

Protium concentrations in thermonuclear reactor fuel streams will probably have to be reduced to 1% or less. The D/T isotopic ratio must be adjusted by the addition of medium deuterium.

Clearly, external deuterium requirements for fusion power plants will be a significant part of the tritium fuel cycle. The amount of deuterium required will be affected by the presence of tritium and deuterium. A significant amount of the deuterium must be used to offset the presence of the other fuel isotopes. The amount of deuterium required will be affected by the presence of tritium and deuterium. A significant amount of the deuterium must be used to offset the presence of the other fuel isotopes.

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Our discussion will be confined to the dilute-solution conditions anticipated for tritium in fusion reactor breeding blankets, coolant loops, structural materials, and perhaps cavity exhaust streams. Early estimates of rates of tritium escape into steam cycles from coolant loops suggested that tritium concentrations in fusion reactor systems might have to be maintained at 1 ppm or less. As the difficulties of tritium recovery from solutions at such concentrations have become apparent, more effective concepts for prevention of tritium escape have been developed, and the importance of potential tritium hazards relative to other potential fusion reactor hazards have been more accurately assessed, so that a justification has been given to operation with tritium concentrations an order or two higher in magnitude. Nonetheless, dilute solution theory will still be applicable, at least possible higher possible concentrations are still quite low.

We will focus on the development of mixing rules for equilibria of tritium isotopic mixtures, and on the effects that the presence of more than one hydrogen isotope has on the partitioning of tritium in binary systems.

**PHYSICS AND CHEMISTRY OF HYDROGEN ISOTOPIC MIXTURES IN METALS**

Most of the literature of fusion reactors will probably be devoted to the study of problems involving liquid-state systems, including tritium-bearing coolants and primary coolant loops. Clearly, the solubility of tritium, as affected by the presence of other hydrogen isotopes, is critical to the extent in determining tritium concentrations and the performance of tritium recovery systems and breeding blankets. We will discuss some aspects of the equilibria of hydrogen isotopes in metals.

**Review of Equilibria of Hydrogen Isotopes in Metals and a Theoretical Treatment**

Many careful studies have been made by Ricca,<sup>(1)</sup> Ricca,<sup>(2)</sup> and Ricca and Kell,<sup>(3)</sup> Hank,<sup>(4)</sup> and Ricca and Ricca,<sup>(5)</sup> and Ricca and Vassilios,<sup>(6)</sup> have confirmed that the empirical

relationship named for A. Sieverts accurately describes the temperature-dependent solubility of protium, deuterium, and tritium in metals at very low concentrations and, in some instances, at relatively high concentrations, for both pure metals and alloys with low surface-to-volume ratios so that adsorption is not a significant factor.

A theoretical justification for Sieverts' empirical law can be developed as follows. We assume, in accord with experimental evidence, e.g., see Isenberg,<sup>(7)</sup> that a hydrogen solution exists in solution in metals as an interstitial solid solution. For present purposes, it is not necessary whether the dissociation of dihydrogen is necessary for dissolution occurs in the gas phase, on the metallic surface, or in the bulk metal. An equilibrium expression for the interstitial solution is

$$H_2(g) \rightleftharpoons 2H_{int}(M) \quad (1)$$

$$K = \frac{a_{H_{int}}^2}{p_{H_2}} \quad (2)$$

The complete dissociation of dihydrogen in the gas phase is assumed, and the activity of dihydrogen is taken to be unity. Hence, the equilibrium constant is the square of the activity of interstitial hydrogen. The activity of interstitial hydrogen is defined as the product of the mole fraction of interstitial hydrogen and the activity of the pure interstitial hydrogen,  $a_{H_{int}} = x_{H_{int}} a_{H_{int}}^0$ . The activity of the pure interstitial hydrogen is defined as the product of the mole fraction of interstitial hydrogen and the activity of the pure interstitial hydrogen,  $a_{H_{int}}^0 = x_{H_{int}}^0 a_{H_{int}}^{00}$ .

$$K = \frac{x_{H_{int}}^2 a_{H_{int}}^{00}}{p_{H_2}} \quad (3)$$

$$K = \frac{x_{H_{int}}^2 a_{H_{int}}^{00}}{p_{H_2}} \quad (4)$$

If temperature is constant, it is seen that the standard Gibbs free energy of formation of the

ed, then Stevarts' law for the solubility of hydrogen isotopes in metals is obtained:

$$X_{H(s)} = K_{S_H} (T) \left[ P_{H_2} / 1 \text{ atm} \right]^{1/2}$$

$$K_{S_H} (T) = K_{S_H}^0 \exp \left( -Q_{S_H} / RT \right) \exp \left( \frac{V_H^0}{RT} \right) \exp \left( \frac{\Delta S_H^0}{R} \right)$$

$$Q_{S_H} = -\Delta H^0$$

Derivation of Stevarts' law

It is assumed that the only other possible consideration of the problem of predicting solubility of the individual hydrogen isotopes in a solution and the gross solubility in the solution is that the gas solubility in an alloy is a function of the partial pressures of the isotopes. It is assumed that the partial pressures of the isotopes in a solution are proportional to their partial pressures in the gas phase. Stevarts' law is then derived as follows:

$$X_{Total} = \frac{X_{H(s)} + X_{D(s)} + X_{T(s)}}{1}$$

By further assuming that the solubility of hydrogen is

$$X_{H(s)} = K_{S_H} (T) \left[ P_{H_2} / 1 \text{ atm} \right]^{1/2}$$

It is assumed that only a limited number of holes in the lattice are available for hydrogen isotopes. It is assumed that the total number of holes is constant and that both isotopes must occupy the same holes.

Hickman et al. present experimental data for the solubility of hydrogen in a number of metals and alloys. The results of these experimental results, when fitted to the postulated mixing rule, revealed the solubility of the isotopes acceptably well.

Askenov et al. have used the mixing rule suggested by Hickman in analyzing the results of

experiments which investigated the permeation of stellar mixtures through the walls of tubes of the same alloy. They claimed acceptable agreement between their experimental results and those of analysis based on Hickman's suggested mixing rule.

However, the fact that Stevarts' law accurately predicts the solubility of hydrogen isotopes in many metals and alloys up to relatively high concentrations, suggests, for systems sufficiently dilute in the dissolved hydrogen isotopes, that the systems are also relatively dilute in comparison to the number of holes in lattice valence bands. The large isotopic differences in solubility, as reflected by differences in Stevarts' law constants, suggest that a mixture of hydrogen isotopes cannot be treated as a single chemical substance for all purposes. Therefore, the following analysis, which explores the consequences of validity of Stevarts' law for dissolution of individual hydrogen isotopes in metals, was performed to develop an alternative, which has some theoretical basis, to Hickman's solubility mixing rule.

On an atomic basis, in solutions sufficiently dilute in all solutes, solute atoms are surrounded by and interact with virtually all the time with solvent atoms rather than with other solute atoms. Therefore, in such solutions the solubility of any solute is assumed to be determined primarily by its properties and by those of the solvent and to be unaffected directly by the properties of other solutes. This interpretation should also be valid if the solvent is a mixture of elements, as long as one studies only concentrations of the species in the solvent which are constant, namely, if the solvent is an alloy, dilute or otherwise.

Thus we conclude that Stevarts' law expressions obtained by fitting experimental solubility data for pure isotopes are applicable to individual isotope solubilities when isotopic mixtures are involved. Therefore, for a system containing all three hydrogen isotopes, we write:

$$X_{Total} = X_{H(s)} + X_{D(s)} + X_{T(s)} \\ = K_{S_H} (T) \left[ P_{H_2} / 1 \text{ atm} \right]^{1/2} + K_{S_D} (T) \left[ P_{D_2} / 1 \text{ atm} \right]^{1/2} + K_{S_T} (T) \left[ P_{T_2} / 1 \text{ atm} \right]^{1/2}$$







- Equilibrium with respect to isotopic interchange between diatomic molecular hydrogenic species in the gas phase is attained at all times, the high-temperature limiting values of the isotopic interchange equilibrium constants are applicable, and molecular dissociation to give the atomic species can be neglected.

The stated assumptions imply that expressions for the permeation fluxes of protium and tritium through the tritium window can be written in the forms:

$$J_{T_2} = \frac{\sigma_{T_2}(T)}{s} (p_{T_2}^{1/2} - p_{T_2}^{0/2}) = \frac{\sigma_{T_2}(T)}{s} \left[ y_T^2 p_{Total,1}^{1/2} \right]$$

$$= (y_T^2 p_{Total,1}^{1/2}) \frac{D_{T_2}(T)}{l} \frac{M}{M_H} (x_{T_2,1} - x_{T_2,2})$$

$$= \frac{\sigma_{T_2}(T)}{s} \left[ (y_{T_2} p_{Total,1}^{1/2}) - (y_{T_2} p_{Total,2}^{1/2}) \right]$$

$$\sigma_{T_2}(T) = \frac{D_{T_2}(T)}{l} \frac{M}{M_H} \sigma_{T_2}(T)$$

If all these conditions are met, the present analysis, if dissociation of the molecular species to give the atomic species in the gas phase cannot be neglected, then the analysis will be more complex, but similar.

Now let the total pressure on the low-pressure side be negligible and consider the addition of protium to a system containing initially only tritium. Then the ratio of the tritium flux to its initial value is:

$$J_{T_2}/J_{T_2}^0 = y_T^2 (p_{Total,1}/p_{Total,1}^0)^{1/2}$$

whereas the ratio of the effective system tritium inventories under the same conditions is:

$$C_T/C_T^0 = (p_{T_2}^0)^{1/2} p_{H_2}^{1/2} / (p_{T_2}^0)^{1/2} y_T^2 p_{Total,1}^0$$

$$C_T/C_T^0 = p_{T_2}^0 / (p_{T_2}^0)^{1/2} y_T^2 p_{Total,1}^0$$

respectively, for a gas-phase and a liquid-metal phase constituting the principal tritium reservoir.

If the system tritium inventory is maintained constant, then, respectively, for the two cases:

$$y_T^2 p_{Total,1}^0 / p_{Total,1} = y_T^2 (p_{Total,1}^0 / p_{Total,1})^{1/2}$$

$$J_{T_2}/J_{T_2}^0 = y_T^{1/2} = 1, \quad J_{T_2}/J_{T_2}^0 = 1$$

In the first case, although the system tritium inventory has not been reduced, the tritium window area will have to be increased to remove tritium from the system at the same total value. In the second case the isotopic sweeping is not affected the required tritium window area. Thus, depending on what type of phase represents the principal tritium reservoir, the tritium window area required for a constant total rate of tritium recovery is either increased or not affected for a constant tritium inventory, but clearly is increased if the tritium inventory is to be reduced.

If, instead, the total hydrogen isotope pressure is maintained constant, then:

$$J_{T_2}/J_{T_2}^0 = y_T^2 = \lambda$$

in both cases, while respectively:

$$C_T/C_T^0 = y_T, \quad C_T/C_T^0 = y_T^2$$

Thus, in both cases, the tritium window area required to effect the indicated inventory decrease at a constant tritium recovery rate is increased by the factor  $1/\lambda$ , but the tritium inventory reduction is greater in the second case.

It is also clear that isotopic sweeping will either enhance or not affect the performance of barriers to tritium migration for all the cases considered. Note also that the increase in tritium window area required for removal of tritium at a constant rate when no protium is added is  $1/\lambda$  when the tritium inventory level is reduced by the factor  $\lambda$  in either a gas phase or a liquid-metal phase.

### Isotopic Swamping Effects When Surface Processes are Rate Determining

Nickman<sup>(35)</sup> and Varoni<sup>(36)</sup> examined another case of tritium recovery through a tritium window from a fluid stream that had been isotopically swamped with protium. This case involved the postulate that the permeation rate-limiting step was a slow surface process, the recombination of hydrogen isotope atoms followed by desorption from the low tritium partial-pressure side of the membrane. Adsorption-desorption processes, even if consideration is restricted to adsorption and desorption of hydrogen isotopes only, can be complex and there is a vast, often contradictory literature concerning this topic. Therefore, we can only briefly touch upon the subject. If the adsorption and dissociation step on the upstream side of the barrier is permeation rate controlling then a similar approach can be used in the analysis.

This particular step in the permeation process is carefully examined because there is evidence that, under projected thermonuclear reactor conditions, the recombination and desorption of tritium atoms may indeed be rate-limiting. For example, Gondall, et al.,<sup>(37)</sup> explained the results of their experiments concerned with permeation of hydrogen isotopes from liquid lithium through niobium membranes on the basis of such a rate-limiting step.

The model for hydrogen isotope permeation which we shall consider involves the following assumptions, and approximations:

- All resistances to permeation other than those due to the desorption process are negligible.
- The partial pressures of tritium and protium on the low partial pressure side of the barrier are so small that the adsorption rate on that side of the barrier is negligible in comparison to the desorption rate.
- The simple Langmuir adsorption theory with a single class of active sites adequately describes the adsorption process.
- Dissociation in the gas phase to form the atomic hydrogen isotope species from the diatomic molecular species can be neglected.

- The adsorptive characteristics of the high and low partial-pressure barrier surfaces do not differ significantly.
- The permeation occurs under steady-state, isothermal conditions.

The essence of the elementary Langmuir theory of adsorption may be stated as follows. Adsorption of molecules from the gas phase onto solid surfaces can occur only at certain active "sites" on the surface which have an affinity for the species being adsorbed, are uniformly distributed, and have equal affinities for the adsorbed species. Each such site is assumed to be capable of adsorbing only a single atom or molecule of the adsorbed species and, because the forces that are responsible for the adsorption are short range, the adsorption at any site is assumed to be independent of whether or not an adjacent site is occupied. If the adsorption involves a dissociation, say of a diatomic molecule, such as tritium molecules, to form the atomic species, then the adsorption process is assumed to involve a reaction between the diatomic molecule and two adjacent sites on the solid surface. The number of pairs of adjacent sites, based on the above listed characteristics of the active sites, is proportional to the square of the number of unoccupied sites, which can be represented in terms of a fractional occupancy of active sites by the adsorbed species, often called the surface coverage by the adsorbed species. In terms of the surface coverage by the adsorbed species and the partial pressure of the gas phase molecular form, a kinetically third-order expression for the rate of adsorption is postulated:

$$r_{T_2\text{Ads}} = k_{T_2\text{Ads}}(T)(1-\theta_T)^2 p_{T_2}$$

Similarly, the desorption reaction is assumed to involve the kinetically second order reaction of two adsorbed atoms on adjacent active sites whose number is taken as proportional to the square of the fractional coverage and, in terms of surface coverage by the adsorbed species, a rate expression is written as:

$$r_{T_2Des} = k_{T_2Des}(T) \theta_T^2$$

Under conditions of adsorption equilibrium, the two rate expressions for adsorption and desorption can be equated and solved for  $\theta_T$  to obtain:

$$\theta_T = \frac{\left[ \frac{k_{T_2Ads}(T)}{k_{T_2Des}(T) P_{T_2}} \right]^{1/2}}{1 + \left[ \frac{k_{T_2Ads}(T)}{k_{T_2Des}(T) P_{T_2}} \right]^{1/2}}$$

Although other, more complex theories may describe the adsorption behavior in a particular system more accurately, the results obtained with the simple Langmuir theory should be representative and may be the most accurate in some cases, e.g., see Smith, (38) Examples of other types of models for hydrogen isotope adsorption on, and desorption from metals are those of Bucur, et al, (39) and Bucur (40) for adsorption of protium on palladium films. They considered multiple types of active sites and surface reactions and there are many other such treatments. The general approach to analyzing of adsorption or desorption-step-limited permeation processes by using more complex adsorption and desorption models is similar.

The listed assumptions imply that the permeation flux, when only tritium is present, is given by the Langmuir expression for the rate of desorption of tritium from the downstream barrier surface. The surface coverage in the absence of significant upstream surface adsorption and bulk barrier metal diffusive resistances is that corresponding to equilibrium with the upstream molecular tritium partial pressure. The rate expression is therefore:

$$J_{T_2} = \frac{k_{T_2Ads}(T) P_{T_2,1}}{\left\{ 1 + \left[ \frac{k_{T_2Ads}(T)}{k_{T_2Des}(T) P_{T_2,1}} \right]^{1/2} \right\}^2}$$

A similar analysis based on the same assumptions when both tritium and protium are present, can be summarized as follows. The rate expressions are of the form:

$$J_{T_2} = k_{T_2Des}(T) \theta_{T_2}^2 + \frac{1}{2} k_{HTDes}(T) \theta_{T_2} \theta_{H_2}$$

and the adsorption equilibrium expressions are of the form:

$$k_{T_2Ads}(T) \theta_{T_2}^2 + \frac{1}{2} k_{HTDes}(T) \theta_{T_2} \theta_{H_2}$$

$$= k_{T_2Ads}(T) (1 - \theta_{T_2} - \theta_{H_2})^2 P_{T_2,1}$$

$$+ \frac{1}{2} k_{HTAds}(T) (1 - \theta_{T_2} - \theta_{H_2})^2 P_{HT,1}$$

The preceding adsorption equilibrium expression and the gas-phase isotopic interchange equilibrium expression can be solved for the diatomic protium and tritium and HT partial pressures in terms of the protium and tritium atom fractions in the gas phase and of the total hydrogen isotope partial pressure, although the solution may have to be obtained by numerical techniques, and the results inserted into the rate expressions. The presence of the third hydrogen isotope, deuterium, and significant dissociation of the molecular species to form the atomic species in the gas phase further complicate the problem, but the same principles are applicable.

If the tritium is isotopically swamped with protium, we have:

$$P_{H_2} \approx P_{HT} \approx P_{T_2}, \quad \theta_H \approx \theta_T$$

and the rate and adsorption equilibrium expressions become, respectively:

$$J_{T_2} = \frac{1}{2} k_{HTDes}(T) \theta_{T_2} \theta_{H_2} = J_{HT} = k_{H_2Des}(T) \theta_{H_2}^2$$

and:

$$\frac{1}{2} k_{T_2Des}(T) \theta_{T_2}^2 + \frac{1}{2} k_{HTDes}(T) (1 - \theta_{H_2})^2 P_{HT}$$



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and encourage me to the best of my ability to  
assist you in the best of my ability. This is the  
of the best of my ability to assist you.

Very truly yours,

John F. Kennedy

John F. Kennedy  
1000 Massachusetts Avenue  
Washington, D.C. 20004

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The first part of the report discusses the general principles of the theory of the structure of the atmosphere. It is shown that the atmosphere is a fluid medium in which the pressure and density vary with height. The equilibrium of the atmosphere is determined by the balance of forces acting on a small element of the fluid. The forces are the weight of the element, the pressure forces, and the buoyant force. The equilibrium condition is expressed by the hydrostatic equation:

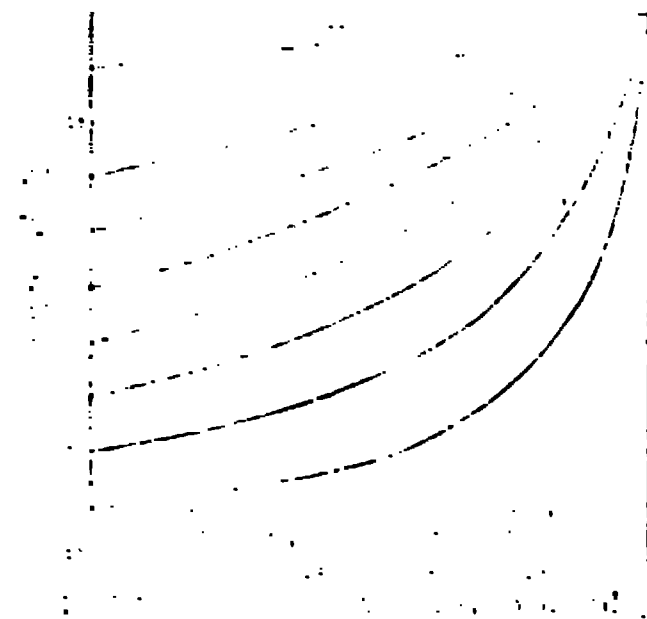
$$\frac{dp}{dz} = -\rho g$$

where  $p$  is the pressure,  $z$  is the height,  $\rho$  is the density, and  $g$  is the acceleration due to gravity. This equation is integrated to give the barometric formula, which relates the pressure to the height. The barometric formula is used to determine the height of a mountain or the depth of a well from a measurement of the pressure.

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where  $p$  is the pressure,  $z$  is the height,  $\rho$  is the density, and  $g$  is the acceleration due to gravity. This equation is integrated to give the barometric formula, which relates the pressure to the height. The barometric formula is used to determine the height of a mountain or the depth of a well from a measurement of the pressure.



- If tritium recovery system performance is determined primarily by transport rates, then isotopic swamping probably is not cost-effective and may be completely useless.
- If tritium recovery system performance is determined primarily by equilibrium considerations, then isotopic swamping may be cost effective, but there is no guarantee that this will be the case.
- Isotopic swamping will either not significantly affect or will enhance the performance of barriers to tritium escape into the biosphere for a specified tritium concentration level. The judgment of cost effectiveness must, of course, involve consideration of changes in, e.g., required recovery system capacity, requirements for isotopic separation, benefits arising from reductions in tritium inventories and in rates of escape of tritium into the biosphere, effects on other fusion reactor systems, potential use of less expensive construction materials, or lower energy consumption, and cost of a unit of recovery system capacity.

#### (CONCLUSIONS)

Because of limitations spread over the length of papers, we were unable to discuss the effects of the unavoidable presence of other hydrogen isotopes and of isotopic swamping on other fusion reactor tritium recovery systems and tritium migration mechanisms within and between fusion power plants. Examples of tritium recovery processes and migration mechanisms for which interesting analyses using similar methods can be performed include:

- the gas kinetic-limited permeation process discussed by Levin and Stickney,<sup>(40)</sup>
- the nonequilibrium permeation process described by Shupe and Stickney,<sup>(51)</sup>
- high-temperature lithium distillation for tritium recovery suggested by Dyle and Wu,<sup>(31)</sup>
- the molten-salt extraction process for tritium recovery from liquid lithium described by Maroni, et al.,<sup>(52)</sup>
- permeation through potential nonmetallic materials of construction for fusion reactors,

- e.g., organic polymeric materials used for, e.g., gaskets and seals, and ceramics, such as those discussed by Fowler, et al.,<sup>(53)</sup> and oxide or other corrosion layers that are potentially useful as tritium barriers, as discussed by Strehlow and Savage,<sup>(52)</sup> and
- thermal diffusion processes discussed by Pendergrass.<sup>(30)</sup>

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**DEFINITIONS**

- C Concentration
- D Diffusivity
- $C_0$  Equilibrium concentration of the gas
- $C^0$  Standard state free energy change
- $H^0$  Standard enthalpy change
- H Partition coefficient and recovery rate
- $J, J^0$  Flux density
- k Adsorption or desorption rate constant
- $k_{app}$  Apparent rate constant
- $k_s$  Surface reaction constant
- $K_s$  Sieverts' law constant
- $K_s^0$  Sieverts' law equilibrium constant
- P Molecular weight

- $R_{Na}$  Sodium flow rates
- $R_{Na}^0$  Sodium flow rates
- P.P Pressure
- $K_2$  Sieverts' law exponential constant
- r Absorption or desorption rate
- R Ideal gas constant
- $S^0$  Standard entropy change
- T Absolute temperature
- $\gamma^0$  Trifluoromethane recovery rate
- X Mole fraction
- $v, v'$  Mole, atom fractions

**Great Letters**

- a Trifluoromethane permeation barrier thickness
- $\gamma$  Activity coefficient
- $\theta$  Fractional surface coverage by adsorbed species
- $\lambda$  Trifluoromethane concentration level
- $\rho$  Density
- $\sigma$  Permeability